

Name: \_\_\_\_\_ Period: \_\_\_\_\_ Date: \_\_\_\_\_

## Review: Classifying Triangles

### Parts of a Triangle:

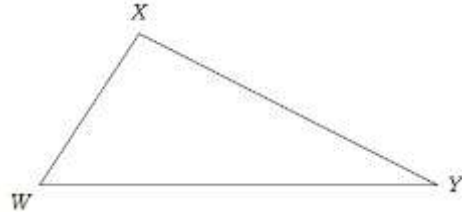
Triangle – a three-sided polygon

Name –

Sides –

Vertices –

Angles –



### Classifying Triangles by Angles:

Acute  $\Delta$

Obtuse  $\Delta$

Right  $\Delta$

Equiangular  $\Delta$  -

### Classifying Triangles by Sides:

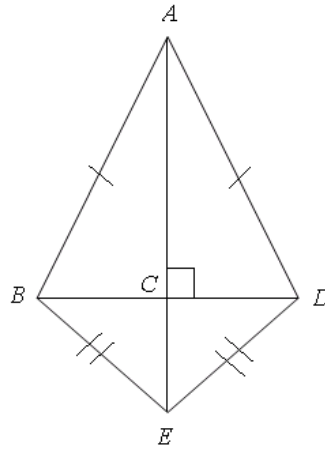
Scalene  $\Delta$

Isosceles  $\Delta$

Equilateral  $\Delta$

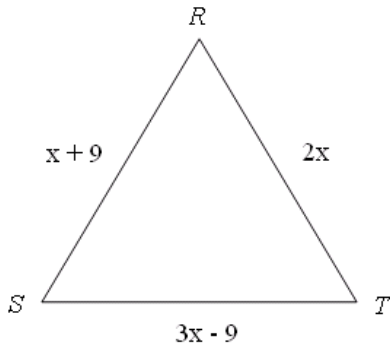
**Example #1:** Identify the indicated type of triangle in the figure.

a.) isosceles triangles

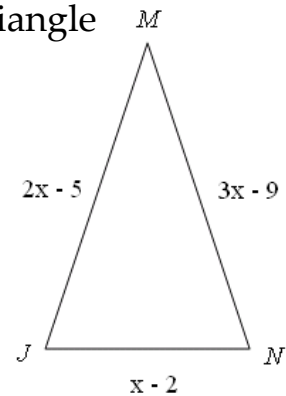


b.) scalene triangles

**Example #2:** Find  $x$  and the measure of each side of equilateral triangle  $RST$ .



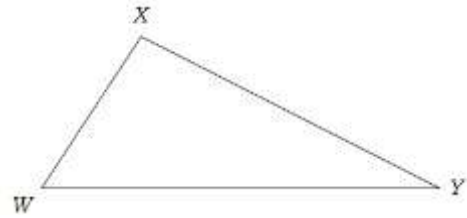
**Example #3:** Find  $x$ ,  $JM$ ,  $MN$ , and  $JN$  if  $\triangle JMN$  is an isosceles triangle with  $\overline{JM} \cong \overline{MN}$ .



## Review: Angles of Triangles

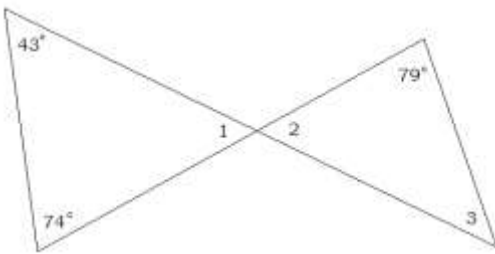
### Angle Sum Theorem:

- The sum of the measures of the angles of a \_\_\_\_\_ is \_\_\_\_\_.

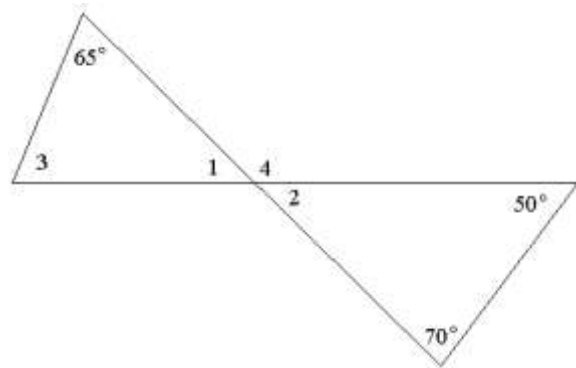


**Example #1:** Find the missing angle measures.

a.)

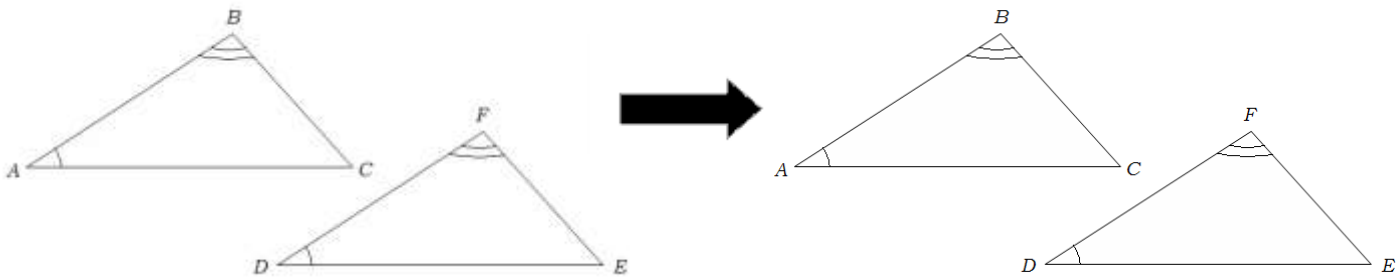


b.)



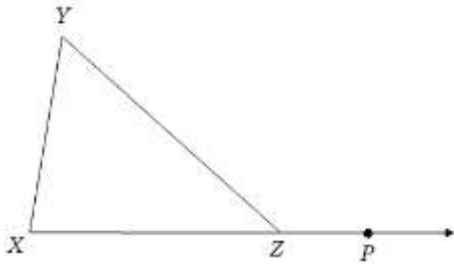
### Third Angle Theorem:

- If two angles of one triangle are \_\_\_\_\_ to two angles of a second triangle, then the third angles of the triangles are \_\_\_\_\_.



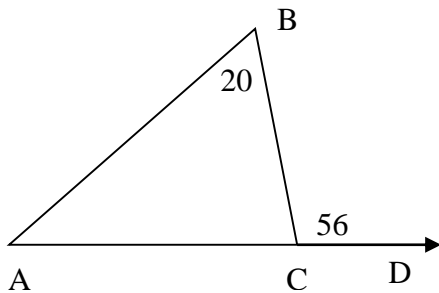
**Exterior Angle Theorem:**

- An **exterior angle** is formed by one side of a \_\_\_\_\_ and the extension of another \_\_\_\_\_.
- **Remote interior angles** are the angles of a triangle that are not \_\_\_\_\_ to a given \_\_\_\_\_ angle.
- The measure of an exterior angle of a triangle is \_\_\_\_\_ to the sum of the measures of the two \_\_\_\_\_ interior angles.



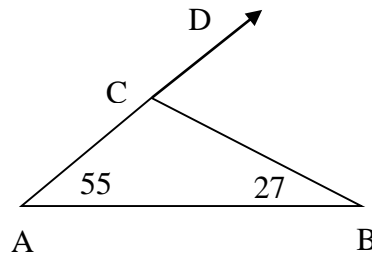
**Example #2:** Find the measure of each of the following angles.

a.)



$m\angle A =$

b.)

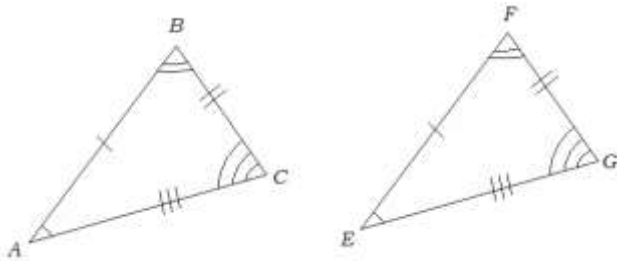


$m\angle DCB =$

## Review: Congruent Triangles

**Congruent Triangles:** triangles that are the same \_\_\_\_\_ and \_\_\_\_\_

- Each triangle has three \_\_\_\_\_ and three \_\_\_\_\_.
- If all \_\_\_\_\_ of the corresponding parts of two triangles are \_\_\_\_\_, then the triangles are \_\_\_\_\_.



*Congruent Triangles:*

*Corresponding Congruent Angles:*

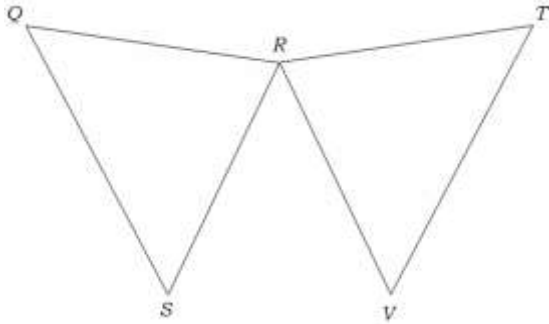
*Corresponding Congruent Sides:*

**Definition of Congruent Triangles (CPCTC):**

- Two triangles are congruent if and only if their corresponding parts are \_\_\_\_\_.
- *CPCTC* - Corresponding parts of congruent triangles are congruent

Name: \_\_\_\_\_ Period: \_\_\_\_\_ Date: \_\_\_\_\_

**Example #1:** In the following figure,  $QR = 12$ ,  $RS = 23$ ,  $QS = 24$ ,  $RT = 12$ ,  $TV = 24$ , and  $RV = 23$ .



Name the corresponding congruent angles and sides.

Name the congruent triangles.

**Properties of Triangle Congruence:**

<u>Reflexive</u>	<u>Symmetric</u>	<u>Transitive</u>

**Example #2:** If  $\triangle WXZ \cong \triangle STJ$ , name the congruent angles and congruent sides.

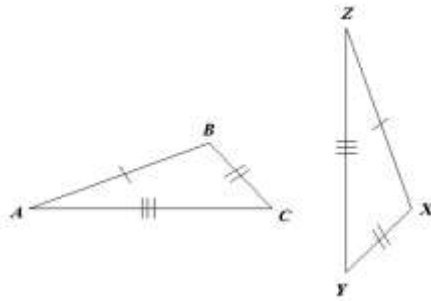
*Angles -*

*Sides -*

**Review: Proving Congruence - SSS, SAS**

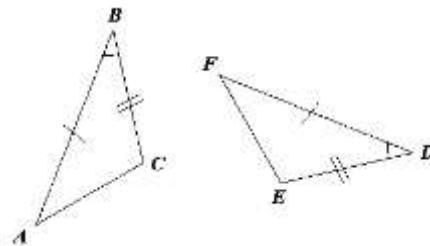
**Side-Side-Side Congruence:** If the \_\_\_\_\_ of one triangle are congruent to the sides of a second triangle, then the triangles are \_\_\_\_\_.

*Abbreviation:*



**Side-Angle-Side Congruence:** If two sides and the included \_\_\_\_\_ of one triangle are congruent to two \_\_\_\_\_ and the included angle of another triangle, then the triangles are \_\_\_\_\_.

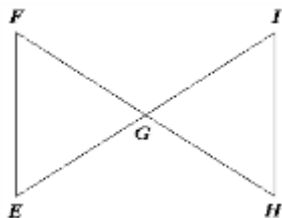
*Abbreviation:*



**Example #1:** Write a proof.

*Given:*  $\overline{EI} \cong \overline{FH}$  ,  $\overline{FE} \cong \overline{HI}$  , and  $G$  is the midpoint of both  $\overline{EI}$  and  $\overline{FH}$  .

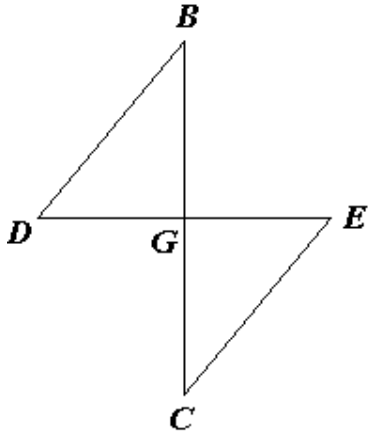
*Prove:*  $\triangle FEG \cong \triangle HIG$



**Example #2:** Write a proof.

*Given:*  $\overline{DE}$  and  $\overline{BC}$  bisect each other.

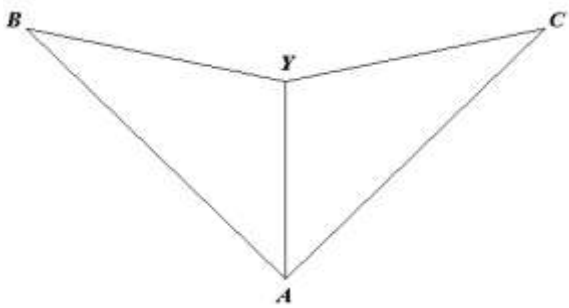
*Prove:*  $\triangle DGB \cong \triangle EGC$



**Example #3:** Write a proof.

*Given:*  $\overline{AB} \cong \overline{AC}$  and  $\overline{BY} \cong \overline{CY}$

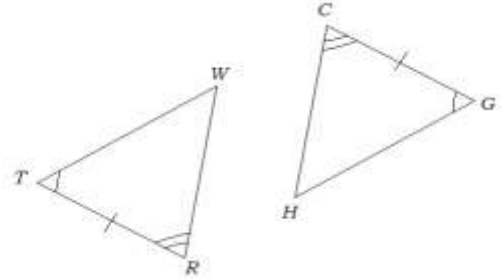
*Prove:*  $\triangle BYA \cong \triangle CYA$





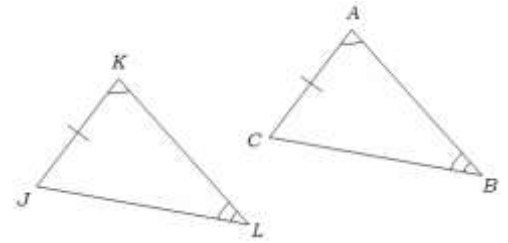
**Review: Proving Congruence - ASA, AAS**

**Angle-Side-Angle Congruence:** If two \_\_\_\_\_ and the included \_\_\_\_\_ of one triangle are congruent to two angles and the included side of another triangle, then the triangles are \_\_\_\_\_.



***Abbreviation:***

**Angle-Angle-Side Congruence:** If two angles and a non-included side of one triangle are congruent to the corresponding two \_\_\_\_\_ and a side of a second triangle, then the two triangles are \_\_\_\_\_.



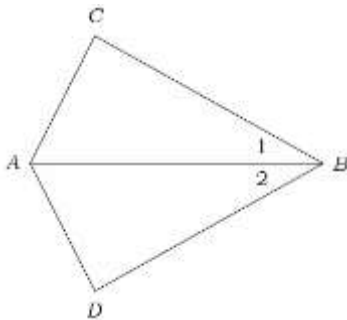
***Abbreviation:***

**Example #1:** Write a two-column proof.

**Given:**  $\overline{AB}$  bisects  $\angle CAD$

$\angle 1 \cong \angle 2$

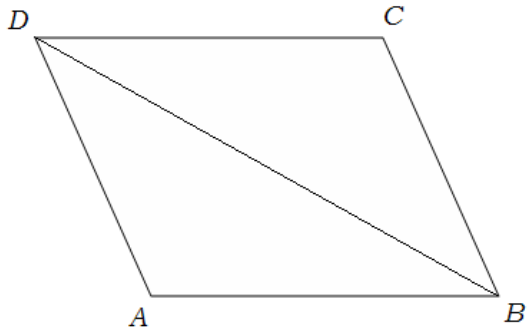
**Prove:**  $\triangle CAB \cong \triangle DAB$



**#2:** Write a two-column proof.

*Given:*  $\overline{AD} \parallel \overline{CB}$   
 $\angle A \cong \angle C$

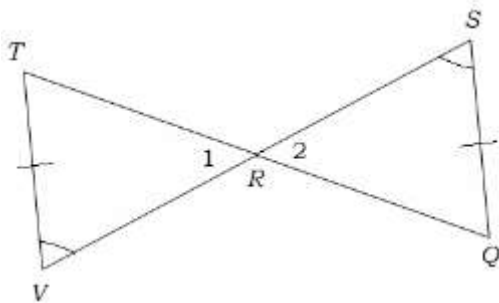
*Prove:*  $\triangle DGB \cong \triangle EGC$



**Example #3:** Write a two-column proof.

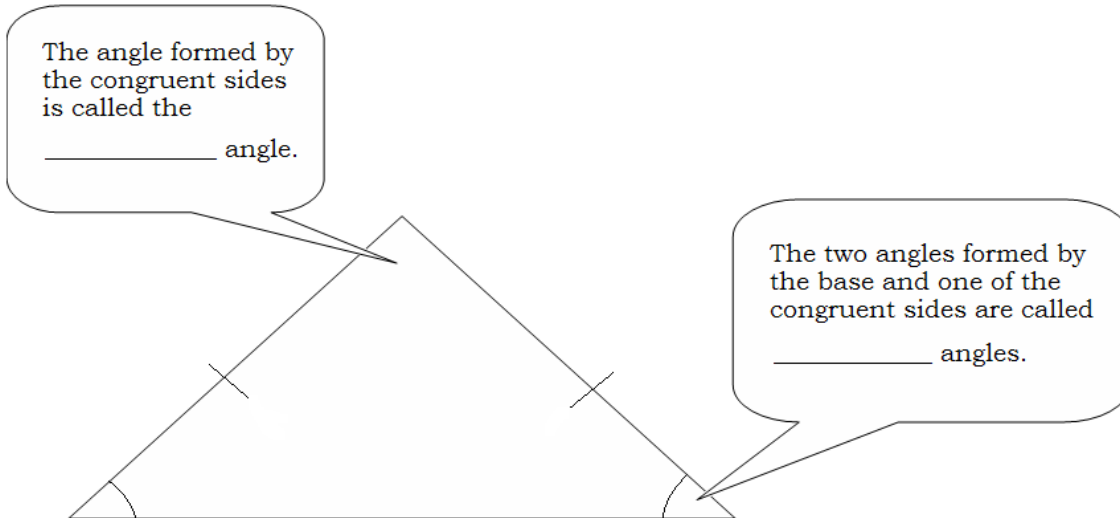
*Given:*  $\angle V \cong \angle S$   
 $\overline{TV} \cong \overline{QS}$

*Prove:*  $\overline{VR} \cong \overline{SR}$



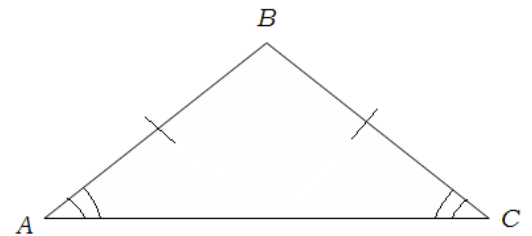
## Isosceles Triangles

**Isosceles Triangle:** A triangle with at least \_\_\_\_\_ sides congruent.

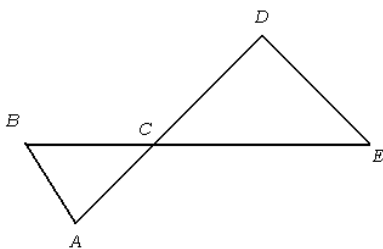


**Isosceles Triangle Theorem:** If two sides of a triangle are \_\_\_\_\_, then the angles opposite those sides are \_\_\_\_\_.

**Ex:**

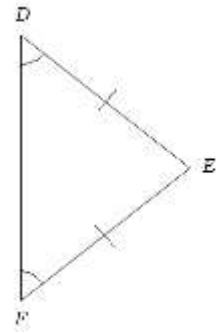


**Example #1:** If  $\overline{DE} \cong \overline{CD}$ ,  $\overline{BC} \cong \overline{AC}$ , and  $m\angle CDE = 120$ , what is the measure of  $\angle BAC$ ?



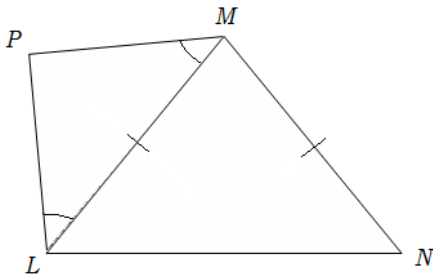
**Theorem:** If two angles of a \_\_\_\_\_ are congruent, then sides opposite those angles are \_\_\_\_\_.

the



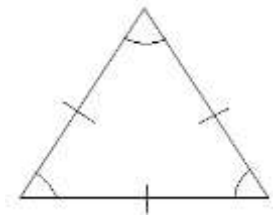
**Ex:**

**Example #2:**

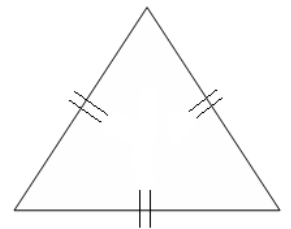


- Name all of the congruent angles.
- Name all of the congruent segments.

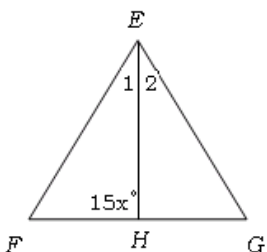
**Corollary:** A triangle is \_\_\_\_\_ if and only if it is \_\_\_\_\_.



**Corollary:** Each angle of an equilateral triangle measures \_\_\_\_\_.



**Example #3:**  $\triangle EFG$  is equilateral, and  $\overline{EH}$  bisects  $\angle E$ .



- Find  $m\angle 1$  and  $m\angle 2$ .
- Find  $x$ .