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TRIANGLE CONGRUENCE USING SSS AND SAS

Unit 4 Lesson 2

## TRIANGLE CONGRUENCE USING SSS AND SAS

## Students will be able to:

identify the congruent triangles using SSS (Side-Side-Side) and SAS (Side-Angle-Side) postulates.

## Key Vocabulary

- Congruent triangles
- Side-Side-Side Postulate
- Side-Angle-Side Postulate


## TRIANGLE CONGRUENCE USING SSS AND SAS

## Congruent triangles

Two triangles are congruent if they have same shape and the same size.

- The corresponding angles of the congruent figures are equal in measures.
- The corresponding sides of the congruent shapes are equal.


Figure 1


Figure 2

The figure $\mathbf{1}$ and figure $\mathbf{2}$ are congruent since both shapes are triangles and their size is same.

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## How to show congruence of two triangles

Suppose you want to see whether two triangles are congruent or not. What information you need? What properties of triangles you can use to show that two triangles are congruent?

The two properties of a triangle are:

- 3 Sides
- 3 Angles

We can use these properties (any valid combination of these properties) to show whether two triangles are congruent or not.

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## The Side-Side-Side Postulate (SSS)

If all the three sides of one triangle are congruent (equal in measures) to all the corresponding three sides of another triangle, then the two triangles are said to be congruent.


The two triangles shown are congruent by SSS postulate since all the sides of one triangle are congruent to the corresponding three sides of the other triangle.

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## Example 1: Show that the two triangles given below are congruent.



From the figure, we see that:


$$
\begin{aligned}
& A B \cong P Q=3 \\
& A C \cong P R=5 \\
& B C \cong Q R=4
\end{aligned}
$$

Since three sides of $\triangle A B C$ are congruent to corresponding three sides of $\triangle P Q R$, so by SSS postulate:

## TRIANGLE CONGRUENCE USING SSS AND SAS

## The Side-Angle-Side Postulate (SAS)

If two sides and their included angle of one triangle is congruent to the two sides and their included angle of another triangle, the two triangles are said to be congruent.


The two triangles shown are congruent by SAS postulate since the two sides and their included angle one triangle is congruent to the two sides and their included angle of the other triangle.

## TRIANGLE CONGRUENCE USING SSS AND SAS

Example 2: Show that the two triangles given below are congruent.


From the figure, we see that:

$$
\begin{aligned}
& A B \cong D F=12 \\
& B C \cong F E=5 \\
& \angle B \cong \angle F=90^{\circ}
\end{aligned}
$$

Since two sides and their included angle of $\triangle \mathrm{ABC}$ is congruent to the two sides and their included angle of $\triangle D E F$, so by SAS postulate:
$\Delta \mathrm{ABC} \cong \triangle \mathrm{DEF}$

